
The Transmission of Foreign Shocks in a Networked Economy

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¹Disclaimer: The views expressed in this presentation are those of the authors and do not necessarily reflect the views of Banco de España, the ECB, or the Eurosystem.

- Recent wave of supply-side **macroeconomic shocks with sectoral and international origins** affecting inflation developments:
 - Energy price increases
 - Supply bottlenecks
 - Covid-19, risks of trade fragmentation , import tariffs ...
- We build a **model that accommodates the disaggregated and international nature of macroeconomic shocks**:
 - Global economy with multiple countries (may form part of currency unions)
 - **Multi-sectoral** productive structure with **national and international production linkages**

- Focus on the **effects and transmission of imported energy prices shocks** in the Euro-Area
 - 1. Significant pass-through to core**, increasing persistence of headline (Adolfson *et al.*, 2024)
 - 2. Contribution of input-output (IO) linkages:**
 - ▶ No IO: headline \approx 60% of baseline, shorter lived, smaller pass-through to core
 - ▶ Upstream sectors drive short-run inflation, downstream long-run inflation
 - 3. Cross-country heterogeneity:**
 - ▶ DE: more downstream industries and long production chains generate larger transmission to core and more persistent headline inflation
 - ▶ ES: higher CPI energy weights increase headline on impact but shorter-lived
 - 4. Implications for monetary policy:**
 - ▶ Weaker response mon. pol. to inflation: IO duplicates increase in inflation volatility
 - ▶ ...despite that IO reduces impact of *mon. pol. shocks* (Nakamura and Steinsson, 2010; Rubbo, 2023)

Model

Model

1. **Model Overview**
2. Households
3. Firms
4. Monetary Authority
5. Market Clearing

Model Overview

- Global economy with **K countries**
 - International financial markets incomplete
 - Monetary arrangements:
 - ▶ $K^{\text{MU}} \subset K$ countries form part of **monetary union** with a common central bank
 - ▶ Remaining countries have monetary autonomy
- Within each country $\mathbf{k} \in \mathbf{K}$
 - **I sectors**: multi-sector productive structure with **national and international networks**
 - **Nominal rigidities** on *prices* (heterogeneous across sectors) and *wages* (homogeneous across sectors)

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Households - Intertemporal Problem

- Representative households' problem in country $k \in K$:

$$\max_{C_{k,t}, \{B_{k,t}^l\}_{l=1}^K} \sum_{t=0}^{\infty} \beta^t \left(\frac{C_{k,t}^{1-\sigma} - 1}{1-\sigma} - \int_0^1 \frac{\mathcal{N}_{gk,t}^{1+\varphi}}{1+\varphi} dg \right) Z_{k,t} \quad \text{s.t.}$$

$$P_{kC,t} C_{k,t} + \sum_{l=1}^K B_{k,t}^l \left[1 - \Gamma(\mathcal{B}_{k,t}^l) \right]^{-1} \mathcal{E}_{kl,t} \leq \sum_{l=1}^K B_{k,t-1}^l \mathcal{E}_{kl,t} (1 + i_{l,t-1}) + \int_0^1 W_{gk,t} \mathcal{N}_{gk,t} dg + \Pi_{k,t} - T_{k,t} - \Xi_{k,t}$$

- $B_{k,t}^l$: Household holdings in country k of bonds issued by country l
- $\mathcal{E}_{kl,t}$: nominal exchange rate between country k and country l
- $\Gamma(\mathcal{B}_{k,t}^l)$: portfolio adjustment costs to stabilize the model (Schmitt-Grohé and Uribe, 2003)

Households – Consumption Baskets

- Consumption C_k : aggregator of energy ($C_{kE,t}$) and non-energy ($C_{kM,t}$) baskets:

$$C_{k,t} = \left[\tilde{\beta}_k^{\frac{1}{\gamma}} C_{kE,t}^{\frac{\gamma-1}{\gamma}} + (1 - \tilde{\beta}_k)^{\frac{1}{\gamma}} C_{kM,t}^{\frac{\gamma-1}{\gamma}} \right]^{\frac{\gamma}{\gamma-1}}$$

- Energy and non-energy: goods produced by energy and non-energy industries

$$C_{kE,t} = \left[\sum_{i \in I_E} \tilde{v}_{ki}^{\frac{1}{\eta}} C_{ki,t}^{\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}, \quad C_{kM,t} = \left[\sum_{i \in I_M} \tilde{v}_{ki}^{\frac{1}{\iota}} C_{ki,t}^{\frac{\iota-1}{\iota}} \right]^{\frac{\iota}{\iota-1}}$$

- Each energy and non-energy good combines varieties produced by different countries:

$$C_{ki,t} = \left[\sum_{l=1}^K \tilde{\zeta}_{kli}^{\frac{1}{\delta}} C_{kli,t}^{\frac{\delta-1}{\delta}} \right]^{\frac{\delta}{\delta-1}}$$

Wage Setting

- In each country k , nominal wages are infrequently reset by a union (Erceg *et al.*, 2000)
 - Wages are different across countries
 - But common across sectors within a country
- **Wage NKPC** for country k (log-linearized):

$$\pi_{wk,t} = \kappa_{wk} (\sigma \hat{c}_{k,t} + \varphi \hat{n}_{k,t} - \hat{w}_{k,t}) + \beta \mathbb{E}_t \pi_{wk,t+1} + u_{k,t}^w$$

- Where $u_{k,t}^w$ is a wage cost-push shock that follows an AR(1) process

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Firms - Production I

- Firm f (sector i , country k) combines labor and intermediates:

$$Y_{fki,t} = A_{ki,t} \left[\tilde{\alpha}_{ki}^{\frac{1}{\psi}} N_{fki,t}^{\frac{\psi-1}{\psi}} + \tilde{\vartheta}_{ki}^{\frac{1}{\psi}} X_{fki,t}^{\frac{\psi-1}{\psi}} \right]^{\frac{\psi}{\psi-1}}$$

- Intermediates X_{fki} combines energy $X_{fkiE,t}$ and non-energy baskets $X_{fkiM,t}$:

$$X_{fki,t} = \left[\tilde{\beta}_{ki}^{\frac{1}{\phi}} X_{fkiE,t}^{\frac{\phi-1}{\phi}} + (1 - \tilde{\beta}_{ki})^{\frac{1}{\phi}} X_{fkiM,t}^{\frac{\phi-1}{\phi}} \right]^{\frac{\phi}{\phi-1}}$$

- Energy and non-energy baskets: goods produced by energy and non-energy industries

$$X_{fkiE,t} = \left[\sum_{j \in I_E} \tilde{v}_{kij}^{\frac{1}{\chi}} X_{fkij,t}^{\frac{\chi-1}{\chi}} \right]^{\frac{\chi}{\chi-1}}, \quad X_{fkiM,t} = \left[\sum_{j \in I_M} \tilde{v}_{kij}^{\frac{1}{\xi}} X_{fkij,t}^{\frac{\xi-1}{\xi}} \right]^{\frac{\xi}{\xi-1}}$$

- Energy and non-energy goods combines varieties produced by different countries:

$$X_{kij,t} = \left[\sum_{j=1}^I \tilde{\zeta}_{klij}^{\frac{1}{\mu}} X_{klij,t}^{\frac{\mu-1}{\mu}} \right]^{\frac{\mu}{\mu-1}}$$

Firms – Price Setting I

- Firms set prices à la Calvo in the **currency of destination** (local currency pricing paradigm, Devereux and Engel 2003)
- **Price NKPC** of sector i in country k **selling to foreign country** l (log-linearized):

$$\pi_{lki,t} = \kappa_{ki}(\widehat{mc}_{ki,t} - \widehat{p}_{lki,t} - \widehat{q}_{kl,t}) + \beta \mathbb{E}_t \pi_{lki,t+1} + u_{ki,t}^p$$

- $\widehat{q}_{kl,t}$ is the real exchange rate between country k and country l , equal to 1 if sold at home; $u_{ki,t}^p$ is a sectoral cost-push shock that follows AR(1) process
- mc_{ki} : **marginal cost** of sector i that will depend on:
 - Domestic wages w_k
 - Prices charged by domestic (p_{kj}) and international suppliers (p_{klj}) on intermediate goods
 - Costs of suppliers (wages, intermediate goods' prices...) through input-output linkages

- We assume there is an exogenous **price wedge** $\tau_{klij,t}$ between the *price set by the exporting firm* $\tilde{P}_{klj,t}$ and the *actual price paid by the importing firm* $P_{klij,t}$:

$$P_{klij,t} = (1 + \tau_{klij,t}) \tilde{P}_{klj,t}$$

- τ_{klij} : **exogenous movements in import prices (e.g. energy) not triggered by changes in economic activity of the exporting country**

$$\tau_{klij,t} = \rho_{1,kl}^{\tau} \tau_{klij,t-1} + \rho_{2,kl}^{\tau} \tau_{klij,t-2} + \varepsilon_{klij,t}^{\tau}$$

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- **Countries not members of a currency union:** Taylor rule that targets *domestic* headline inflation and domestic GDP:

$$i_{k,t} = \rho_{kr} i_{k,t-1} + (1 - \rho_{kr}) \phi_{k\pi} \pi_{k,t} + (1 - \rho_{kr}) \phi_{ky} \hat{y}_{k,t} + \varepsilon_{k,t}^r \quad (1)$$

- **Member countries of a currency union (K^{MU}):**
 - Country $k^{MU} \in K^{MU}$ sets interest rates responding *union-wide* headline inflation and GDP:

$$i_{k^{MU},t} = \rho_{MUr} i_{k^{MU},t-1} + (1 - \rho_{MUr}) \phi_{MU\pi} \pi_t^{MU} + (1 - \rho_{MUr}) \phi_{MUy} \hat{y}_t^{MU} + \varepsilon_{MU,t}^r$$

- Remaining countries in K^{MU} peg their nominal exchange rate to k^{MU} :

$$\mathcal{E}_{k,k^{MU},t} = \mathcal{E}_{k,k^{MU}} \quad \forall k \in K^{MU}$$

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Market Clearing & GDP

- Labor market clears:

$$N_{k,t} = \sum_{i=1}^I N_{ki,t}$$

- Goods' market clears:

$$Y_{ki,t} = \sum_{l=1}^K \left(C_{lki,t} + \sum_{j=1}^I X_{lkji,t} \right) \quad \forall i \in I$$

- Bonds' market clears:

$$\sum_l B_{l,t}^k = 0, \quad \forall k \in K$$

- Nominal GDP $\mathcal{Y}_{k,t}$:

$$\mathcal{Y}_{k,t} = P_{kC,t} C_{k,t} + P_{kEXP,t} EXP_{k,t} - P_{kIMP,t} IMP_{k,t}$$

- Real GDP:

$$Y_{k,t} = \frac{\mathcal{Y}_{k,t}}{P_{kY,t}}$$

Calibration

Calibration – I

- Calibrate the model to **6 countries** ($K = 6$) and **44 sectors** within each country ($I = 44$):
 - Euro-Area: Spain (ES), Germany (DE), Italy (IT), France (FR), Rest of the Euro Area (REA)
 - Rest of the World
- Calibrate heterogeneous **price frequency adjustments** for each sector and country using data from Gautier *et al.* (2024)
- We linearize the model *by hand* so we can **read input-output matrix, labor shares, and consumption shares directly from the data** (ICIO Input-Output Tables, OECD; and Figaro, Eurostat)

Calibration – II

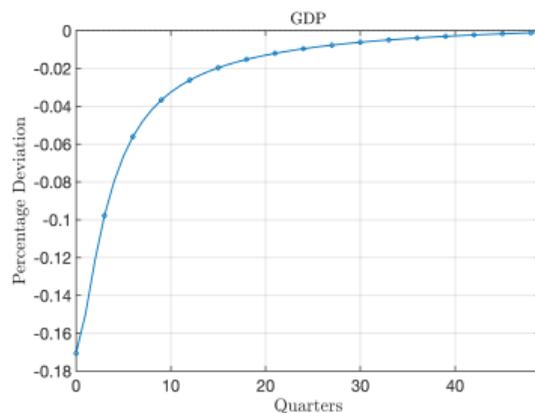
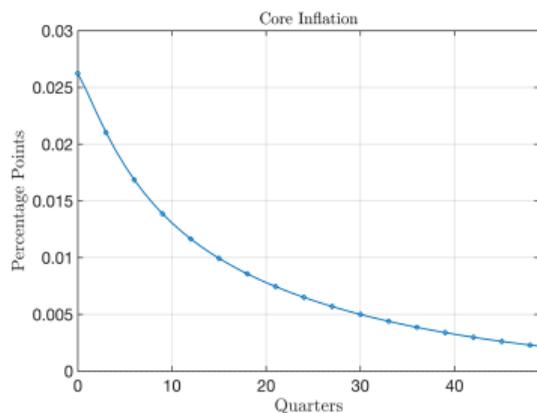
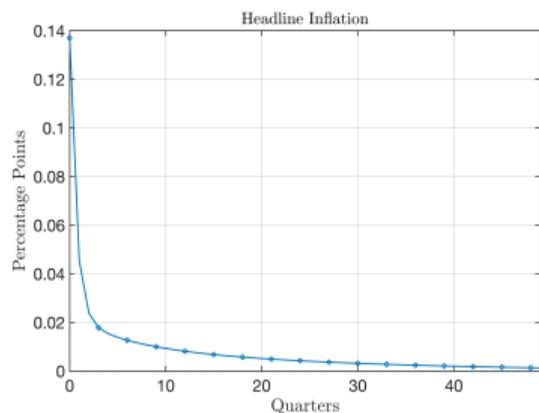
Parameter	Description	Value	Target / Source
Households			
β	Discount factor	0.99	$R = 4.5\%$ p.a.
σ	Inv. Intertemp. Elast. Subs.	1	Standard Value
φ	Inv. Frisch Elasticity	1	Chetty <i>et al.</i> (2011)
γ	Elast. Subst. E and M	0.4	Böhringer and Rivers (2021)
η	Elast. Subst. E	0.9	Atalay (2017)
ι	Elast. Subst. M	0.9	Atalay (2017)
δ	Trade Elasticity	1	Standard value
$\{\tilde{\beta}_k, \tilde{\nu}_{ki}, \tilde{v}_{ki}, \tilde{\zeta}_{kli}\}$	Quasi-shares consumption		ICIO tables (OECD)
θ_k^w	Calvo wage prob.	0.75	Christoffel <i>et al.</i> (2008)
Monetary Policy			
$\rho_{k,r}$	Interest Rate Smoothing	0.7	Standard Value
$\phi_{k,\pi}$	Reaction to Inflation	1.5	Galí (2015)
$\phi_{k,y}$	Reaction to real GDP	0.125	Galí (2015)

Calibration – III

Parameter	Description	Value	Target / Source
Firms			
ψ_{ki}	Returns to scale	1	Constant returns to scale
ψ	Elast. Subst. N and X	0.5	Atalay (2017)
ϕ	Elast. Subst. E and M	0.4	Böhringer and Rivers (2021)
χ	Elast. Subst. M	0.2	Atalay (2017)
ξ	Elast. Subst. E	0.2	Atalay (2017)
μ	Trade Elasticity	1	Standard value
$\{\tilde{\alpha}_{ki}, \tilde{\vartheta}_{ki}, \tilde{\beta}_{ki}, \tilde{\nu}_{kij}, \tilde{v}_{kij}, \tilde{\zeta}_{kij}\}$	Quasi-shares production		ICIO tables (OECD)
\mathcal{M}_{ki}	Markups		Labor shares (Eurostat)
θ_{ki}^p	Calvo price prob.		Gautier <i>et al.</i> (2024)
Exogenous Shock Processes			
$\rho_{1,kli}^\tau$	Persistence price wedge shock	1.17	Brent crude oil
$\rho_{2,kli}^\tau$	Persistence price wedge shock	-0.2	Brent crude oil
σ_{kli}^τ	Std. Dev. price wedge shock	1	Standard Value

Results

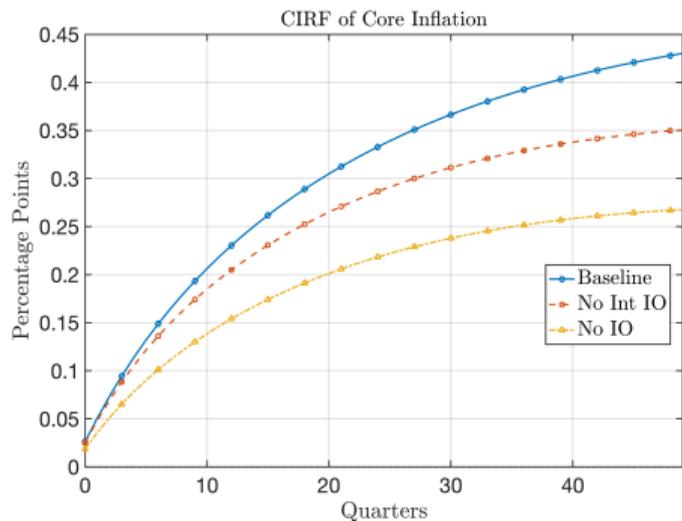
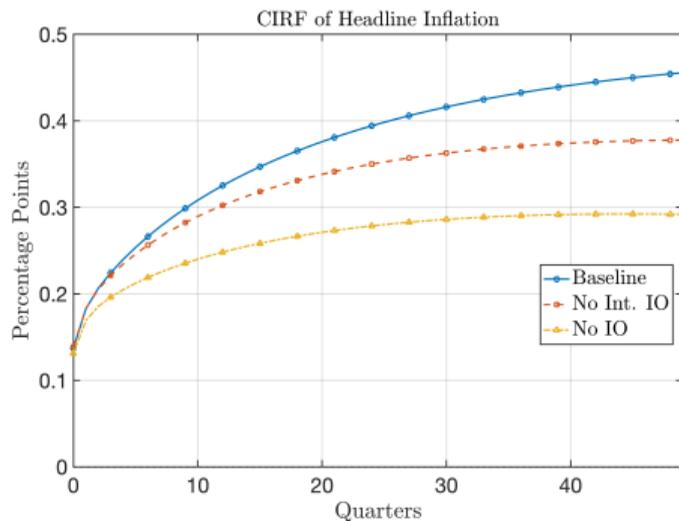
The Transmission of an Increase of Energy Prices



Notes: IRFs to a 10% increase in import energy prices for Euro-Area wide variables.

- Energy shock: large spike of headline inflation on impact which *dies out slowly*
- Significant **pass-through to core inflation** ($\approx 20\%$ of headline) responsible for inflation persistence (Adolfson *et al.*, 2024)

The Role of Production Networks - I



Notes: Cumulative IRF of headline (left panel) and core (right panel) inflation for the baseline and turning off the full, international, or national input-output structure. When turning off the IO structure, we always keep the use of energy as an intermediate input.

- **Without IO:** inflation dies much faster, responding $\approx 60\%$ (cumulative) of baseline with full IO
- **International** production networks (spillovers) important in driving the effects ($\approx 20\%$)

The Role of Production Networks - II

- **For intuition:** domestic currency pricing, fixed nominal exchange rates, and $\tau_{klij t} = \tau_{lj t}$.
- With sticky prices, intermediate goods' prices **inherit persistence from past inflations and shocks**, amplified through **IO linkages**:

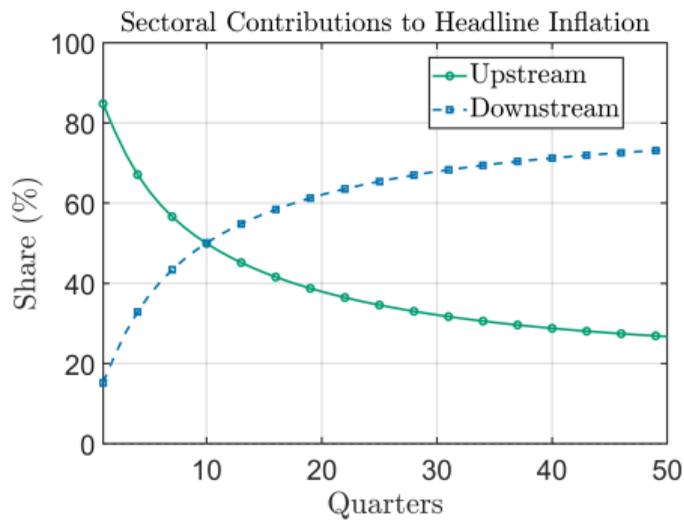
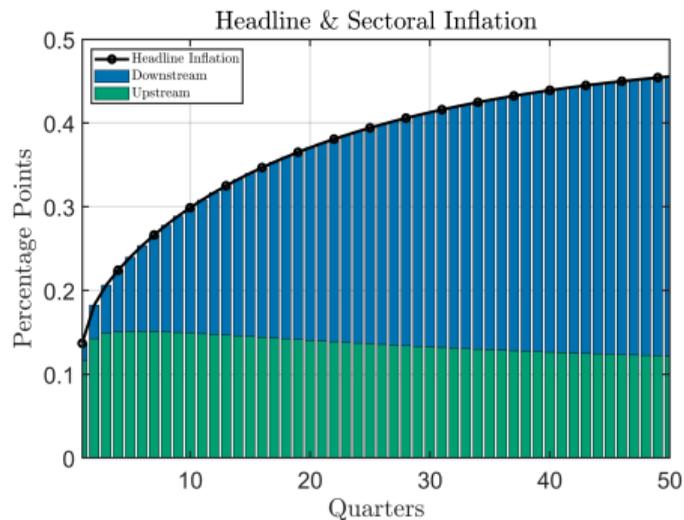
$$p_{t+h} = (I - \Delta\Omega)^{-1} \left[\Delta\Omega R^h \tau_t + (I - \Delta) \sum_{s=1}^h \pi_{t+h-s} + \Delta\alpha \sum_{s=0}^h \pi_{t+h-s}^w + \Delta K^{-1} \beta \mathbb{E}_t \pi_{t+h+1} \right]$$

$\Omega \equiv$ input-output, $K \equiv$ Slope PC, $\Delta = (I - K)^{-1}K$, $\alpha \equiv$ labor share, $R \equiv$ Shock persistence,

- **Rigidity-adjusted Leontief inverse $(I - \Delta\Omega)^{-1}$ amplifies**
 - The impact and **exogenous persistence** of shock $\Delta\Omega R^h \tau_t$
 - ...and the **intrinsic persistence** induced by staggered price- and wage-setting
- More persistent dynamics of prices feed into firms' marginal costs and hence inflation:

$$\widehat{mc}_t^n = \alpha w_t + \Omega (\tau_t + p_t)$$

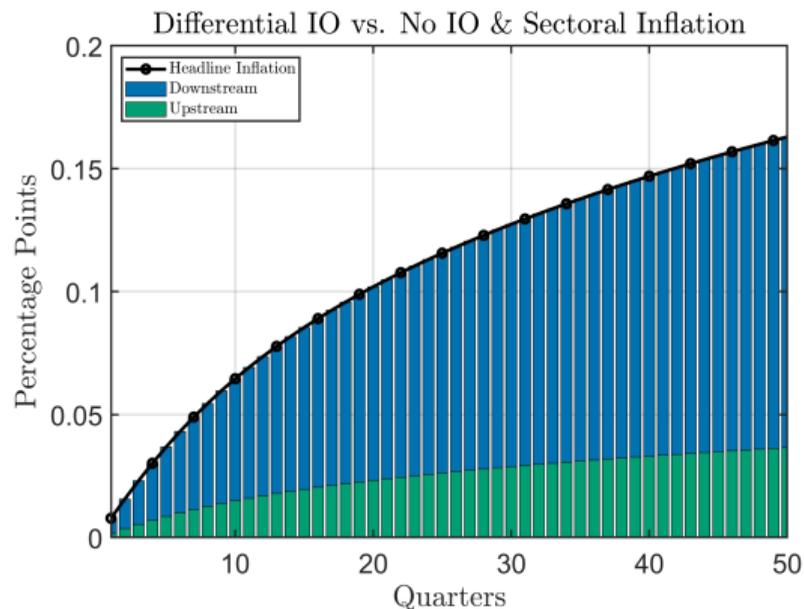
The Role of Production Networks - III



Notes: Left panel: CIRF of headline inflation and contributions of upstream and downstream sectors (Antràs *et al.*, 2012). Right panel: contributions of upstream and downstream sectors as a percent of total headline inflation.

- Short-run inflation dynamics are driven by upstream sectors, but decaying over time
- Downstream sectors drive the persistent increase of headline inflation over time, accounting for up to 80% of headline inflation

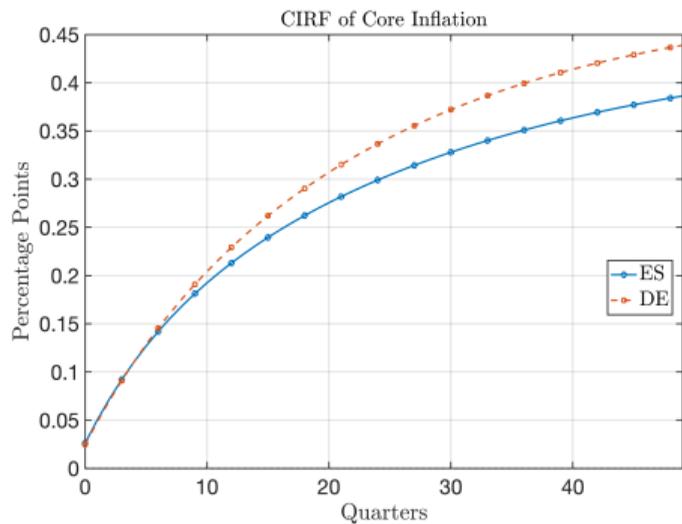
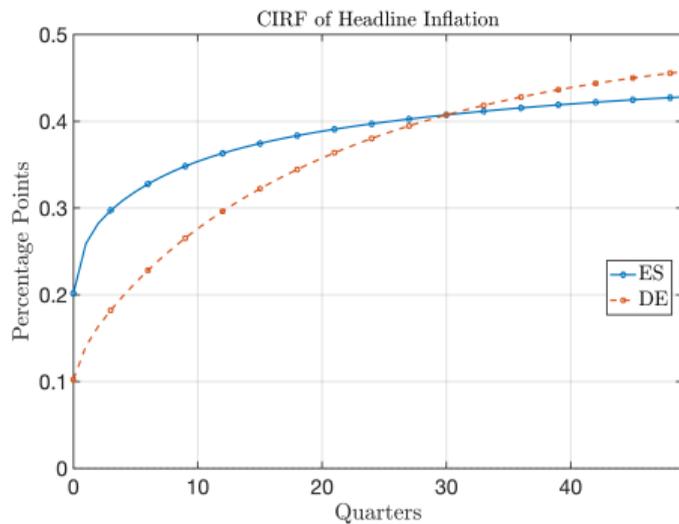
The Role of Production Networks - IV



Notes: CIRF of headline inflation in the baseline with IO minus the CIRF of headline inflation in the counterfactual without IO, and contributions to this difference of upstream and downstream sectors.

- Downstream sectors drive the majority of inflation amplification through production networks

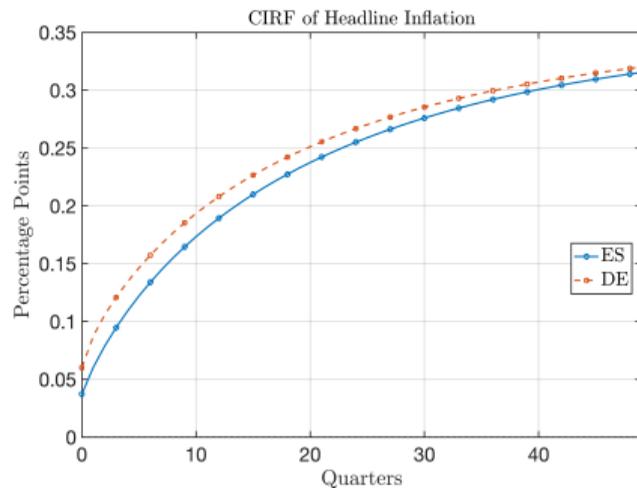
Cross-Country Heterogeneity - I



Notes: Cumulative IRF of headline (left panel) and core (right panel) inflation for Spain (ES) and Germany (DE).

- **ES** strongest headline response on impact but dies out the quickest: *large weight of energy in CPI* but with more *upstream production structure* core inflation raises the least
- **DE** shows the opposite: less weight of energy in CPI but with *downstream and long production chains*

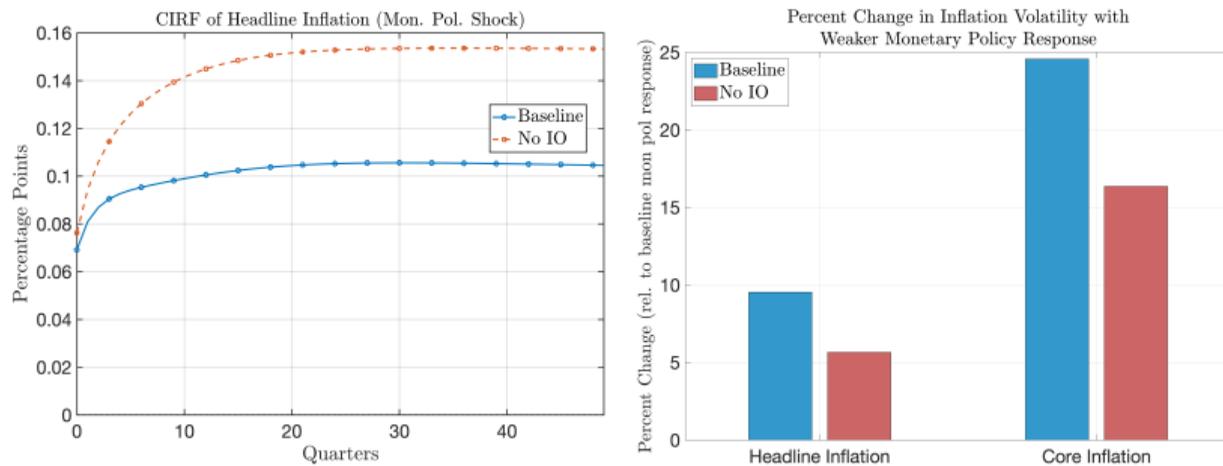
Cross-Country Heterogeneity - II



Notes: Cumulative IRF of headline inflation under common IO structure for Spain (ES) and Germany (DE).

- **Homogenizing** the IO structure reduces the gap between headline inflation dynamics in ES vs. DE
- Remaining difference explained through (slightly) **more flexible prices** in DE

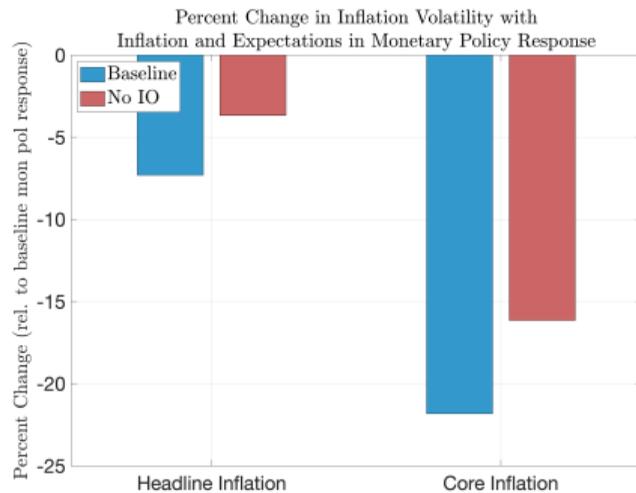
The Interaction Between Monetary Policy and Production Networks - I



Notes: Left panel: CIRF of headline inflation to a monetary policy shock (easing) in the baseline and without IO. Right panel: percent change in inflation volatility (conditional on energy price shocks) with a lower coefficient on inflation in the Taylor rule.

- **Production networks amplify the increase of inflation volatility** from a weaker mon. pol. response
- Despite production networks generating *more* monetary non-neutrality (Nakamura and Steinsson, 2010; Rubbo, 2023)

The Interaction Between Monetary Policy and Production Networks - II



Notes: Percent change in inflation volatility (conditional on energy price shocks) adding inflation expectations in the Taylor rule.

- Reacting to expected inflation reduces volatility **by more** under IO
- **IO induces persistence** in inflation, amplifying the sensitivity of expected inflation and policy rate

Conclusions

Conclusions

- We provide an international multi-sector macroeconomic model with input-output linkages that can accommodate the disaggregated and international nature of macroeconomic shocks
- We analyze the impact and transmission of rising imported energy prices:
 - Production networks important transmission channel to core inflation, increasing persistence of inflation dynamics
 - Heterogeneity in production structures gives rise to cross-country heterogeneity in inflation developments
 - Production networks amplify the increase in inflation volatility resulting from a weaker systematic response of monetary policy to inflation

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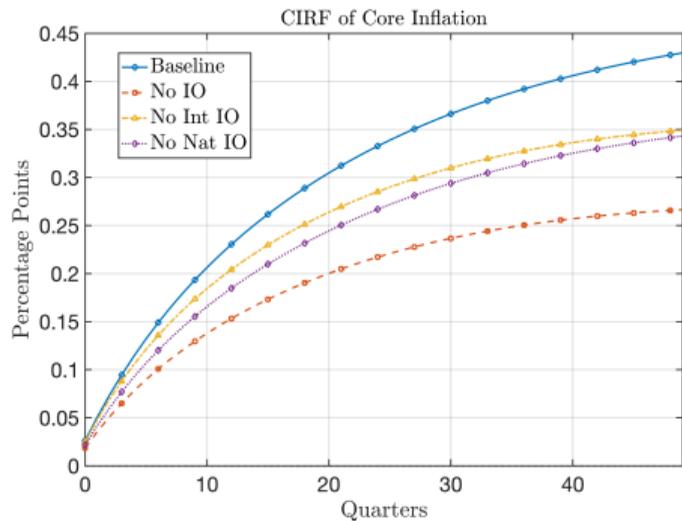
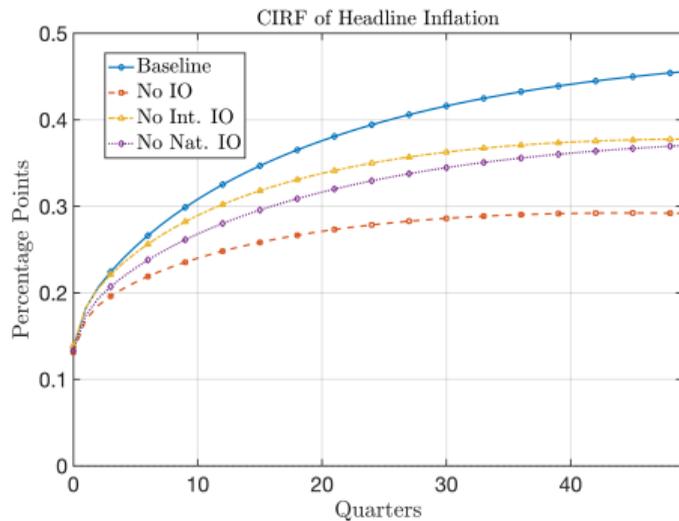
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The Role of Production Networks - AI



Notes: Cumulative IRF of headline (left panel) and core (right panel) inflation for the baseline and turning off the full, international, or national input-output structure. When turning off the IO structure, we always keep the use of energy as an intermediate input.